MATRICES

1 MARK QUESTIONS

- **1.** If A and B are symmetric matrices of the same order, then (AB'-BA) is a
 - (A) symmetric matrix
 - (B) null matrix
 - (C) diagonal matrix
 - (D) skew symmetric matrix

[March, 2025]

- **2.** If matrix $A = \begin{bmatrix} a & b & -5 \\ c & d & 0 \\ 5 & 0 & 0 \end{bmatrix}$ is skew-symmetric,
 - then value of 2a + b + c 3d is
 - (A) 1
- (B) -1
- (C) 0
- (D) 2

[SQP, 2021-22]

- 3. If $A = \begin{bmatrix} 1 & 0 \\ -2 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} -5 & 10 \\ -10 & -5 \end{bmatrix}$, then AB

- $\begin{array}{ccc} \text{(A)} \begin{bmatrix} -5 & -10 \\ 0 & -5 \end{bmatrix} & \text{(B)} \begin{bmatrix} 0 & -5 \\ 25 & 10 \end{bmatrix} \\ \text{(C)} \begin{bmatrix} 10 & -25 \\ -5 & 0 \end{bmatrix} & \text{(D)} \begin{bmatrix} -5 & 10 \\ 0 & -25 \end{bmatrix} \\ \end{array}$

- **4.** If $\begin{bmatrix} x + y & x + 2 \\ 2x y & 16 \end{bmatrix} = \begin{bmatrix} 8 & 5 \\ 1 & 3y + 1 \end{bmatrix}$, then the values of x and y are:

- (A) x = 3, y = 5 (B) x = 5, y = 3 (C) x = 2, y = 7 (D) x = 7, y = 2 [March, 2023] 5. If $P = \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}$, $Q = \begin{bmatrix} x & 0 \\ 1 & 1 \end{bmatrix}$ and $P = Q^2$, then xequals
 - $(A) \pm 1$
- (C) 1

6. Assertion (A): Matrix $A = \begin{bmatrix} 0 & -6 & 7 \\ 6 & 5 & -1 \\ 0 & 0 & 1 \end{bmatrix}$ is a

skew-symmetric matrix.

Reason (R): A matrix A is skew-symmetric if A' = -A.

- 7. If $A = \begin{bmatrix} 4 & 1 \\ 3 & 2 \end{bmatrix}$ and $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$, then $(A^2 6A)$ is equal to:
 - (A) 3I
- (B) -5I
- (C) 5I
- (D) -3I

[July, 2024]

8. If A and B are two matrices such that AB = Aand BA = B, then B^2 is equal to:

- (a) B
- (b) A
- (c) I
- (d) O

[July, 2023]

- **9.** If $A = \begin{bmatrix} 5 & x \\ v & 0 \end{bmatrix}$ is a symmetric matrix, then
 - (A) x = 0, y = 5
- (C) x = y

[July, 2023]

Let $A = \begin{bmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$ The only correct 10.

statement about the matrix A is:

- (A) $A^2 = I$
- (B) A' = -I
- (C) |A| = 0
- (D) A is a scalar matrix [SQP, 2025-26]

If A and B are two square matrices such that $B = -A^{-1}BA$, then $(A + B)^2$ is equal to

(A) O

- (B) $A^2 + B^2$
- (C) $A^2 + B^2 + 2AB$
- (D) $A^2 + B^2 2AB$

For two matrices $P = \begin{bmatrix} 3 & 4 \\ -1 & 2 \end{bmatrix} & Q^T = \begin{bmatrix} 3 & 4 \\ 0 & 1 \end{bmatrix}$

 $\begin{bmatrix} -1 & 2 & 1 \\ 1 & 2 & 3 \end{bmatrix}$; (Where Q^T is the transpose of the matrix Q), P - Q is

- (A) $\begin{bmatrix} 2 & 3 \\ -3 & 0 \\ 0 & -3 \end{bmatrix}$ (B) $\begin{bmatrix} 4 & 3 \\ -3 & 0 \\ -1 & -2 \end{bmatrix}$ (C) $\begin{bmatrix} 4 & 3 \\ 0 & -3 \\ 1 & 2 \end{bmatrix}$ (D) $\begin{bmatrix} 2 & 3 \\ 0 & -3 \\ 0 & 3 \end{bmatrix}$

[SQP, 2024-25]

13. Assertion(A): $A = [aij] = \begin{cases} m; & i = j \\ 0; & i \neq j \end{cases}$

where m is a scalar, is an identity matrix if m

Reason (R): Every identity matrix is not a scalar matrix.

[SQP, 2024-25]

- If AB = A and BA = B, then $(B^2 + B)$ 14. equals:
 - (A) 2A
- (B) O
- (C) 2I
- (D) 2B

[March, 2024]

2 MARKS QUESTIONS

If $A = \begin{bmatrix} 1 & 0 \\ -1 & 7 \end{bmatrix}$, find the value of k such 15. that $A^2 - 8A + kI = 0$.

[2M, March, 2024]

16. Given
$$A = \begin{bmatrix} 2 & 0 & 1 \\ 3 & 4 & 5 \\ 0 & 2 & 3 \end{bmatrix}$$
 and $B = \begin{bmatrix} 1 & 1 & -5 \\ -5 & 1 & -5 \\ 1 & -2 & 4 \end{bmatrix}$, find BA.

[2M,March, 2025]

17. If
$$\begin{bmatrix} x-y & 2x+z \\ 2x-y & 3z+w \end{bmatrix} = \begin{bmatrix} -1 & 5 \\ 0 & 13 \end{bmatrix}$$
, find the value of x, y, z and w.

[2M,March, 2024]

18. Write the matrix
$$\begin{bmatrix} 7 & -3 & -3 \\ -1 & 1 & 0 \\ -1 & 0 & 1 \end{bmatrix}$$
 as a sum of a symmetric and a skew symmetric matrix.

[2M,July, 2023]

19. If
$$A = \begin{bmatrix} \alpha & 0 \\ 1 & 1 \end{bmatrix}$$
 and $B = \begin{bmatrix} 1 & 0 \\ 5 & 1 \end{bmatrix}$, then find the value of α (if exists) for which $A^2 = B$.

[2M,SQP, 2024-25]

20. If A is a square matrix
$$\begin{bmatrix} 2 & -2 \\ -2 & 2 \end{bmatrix}$$
 such that $A^2 = pA$, then find the value of p. [2M,SQP, 2023-24]

21. If
$$\begin{bmatrix} 0 & a & 3 \\ 2 & b & -1 \\ c & 1 & 0 \end{bmatrix}$$
 is skew-symmetric matrix, then find value of a + b + c. [2M,SQP, 2023-24]

22. Find the value of
$$2x + 3b - c$$
, if $A = \begin{bmatrix} 0 & -1 & 28 \\ a - 8 & 0 & 3b \\ -c + 2 & 2 & 0 \end{bmatrix}$ is skew-symmetric matrix. [2M,SQP, 2022-23]

3 MARKS QUESTIONS

23. Two badminton teams A and B are staying in the same hotel. Team A has 2 male and 3 female players accompanied by 1 coach. Team B comprises of 1 male, 2 female players and 2 coaches. The daily diet requirement (calories and protein) for each person is as given below:

	Calories	Protein
Male Player	2500	65g

Female Player	1900	50g
Coach	2000	54g

Use matrix algebra to calculate the total diet requirement of calories and protein for each team.

[3M,SQP, 2022-23]